



**Few Tricks and Tips for**  
**Class-XII Board Examination (2026)**  
**Subject: PHYSICS**  
**Chapter Name : Variation of a quantity**

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**COMMON MISTAKES**

1. let a relation  $y = x^n$  is given, if  $x$  changes is very small, to find the variation  $y$

$$\frac{dy}{dt} = n \left( \frac{dx}{dt} \times 100 \right) \%$$

Example :

- a) Electrostatic force between two charges is inversely proportional to square between the separation of the charges, if separation increases by 5%, find percentage change of force between the charges ?

$$F \propto \frac{1}{x^2}$$
$$\therefore \frac{dF}{F} \times 100 = -2 \frac{dx}{x}$$
$$= -2 \times 5\%$$
$$= -10\%$$

$\therefore$  decreases by 10% .

- b) If  $q$  amount of charge given to a sphere, and radius of the sphere increases by 2%, find the percentage change of volume charge density of the sphere.

$$\text{Charge density } (\sigma) = \frac{q}{\frac{4}{3}\pi r^3}$$

$$\therefore \frac{d\sigma}{\sigma} = -3 \frac{dr}{r}$$
$$\therefore \frac{d\sigma}{\sigma} = -3 \times 2\%$$
$$= -6\%$$

$\therefore$  Volume charge density decreases by 6% .

- c) If resistance of a conductor increases by 3%, find the percentage change of heat produce in the conductor.

$$H = I^2 R t$$

$$\therefore \frac{dH}{H} = \left( \frac{dR}{R} \times 100 \right) \text{ percentage}$$
$$= 3\%$$

- d) If a charge move perpendicularly with a magnetic field, and if velocity increases by 2%, find the percentage change of radius and time period ?

$$r = \frac{mv}{q\beta}$$
$$\frac{dr}{r} = \left( \frac{dv}{v} \times 100 \right) \%$$
$$= 2\%$$

$$T = \frac{2\pi r}{v} = \frac{2\pi m}{q\beta}$$

Time period will remain same because time period does not depend on velocity.

e) If angular frequency of a A.C circuit increases by 4%, find the percentage of change of inductive reactance and capacitive reactance of the circuit.

$$X_L = \omega L \quad \therefore \frac{dx_L}{X_L} = \left( \frac{d\omega}{\omega} \times 100 \right) \%$$

$$X_C = \frac{1}{\omega C} \quad \therefore \frac{dX_C}{X_C} = - \left( \frac{d\omega}{\omega} \times 100 \right) \%$$

$$= - 4 \%$$

2. If  $y = x^n$  is given, if change of  $x$  greater than 5%, to find the variation of  $y$ , the process is as follows.

Let  $x$  changes by  $a\%$  ( $> 5\%$ )

$$x_i = 100$$

$$\therefore x_f = (100 + 100 \times a\%)$$

$$\frac{\Delta y}{y} \times 100 = \frac{x_f - x_i}{x_i} \times 100$$

Example :

a) If two equal charges are placed at a certain separation, the potential energy of the system is  $U$ . If each charge increases by 10%, find the percentage change by potential energy of the system.

$$U_i = K \frac{q \times q}{r^2} \quad q_i = q$$

$$q_f = q + \frac{q}{10} = \frac{11q}{10}$$

$$U_f = \frac{k \frac{11q}{10} \times \frac{11q}{10}}{r^2}$$

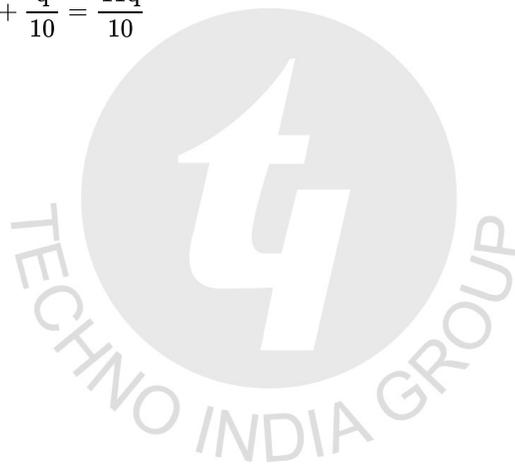
$$= k \frac{121q^2}{100r^2}$$

% change of  $U$

$$= \frac{U_f - U_i}{U_i} \times 100$$

$$= \frac{\frac{121}{100} - 1}{1} \times 100$$

$$= 21\%$$



b) An electron accelerate through a potential difference  $v$ , de Broglie wave length of electron is  $a$ . If potential difference increases by 45%. Find the percentage change of de Broglie wave length ?

$$\lambda \propto \frac{1}{\sqrt{v}}$$

$$\frac{\lambda_1}{\lambda_2} = \sqrt{\frac{v_2}{v_1}} = \sqrt{\frac{144v}{100v}} = \frac{12}{10}$$

$$\therefore \% \text{ change} = \frac{\lambda_1 - \lambda_2}{\lambda_1} \times 100$$

$$= \frac{12 - 10}{12} \times 100$$

$$= \frac{100}{6} \%$$

$$= 16\frac{2}{3} \%$$